

Code.No: R05010202

R05

SET-1

I - B.TECH EXAMINATIONS, DECEMBER – 2010**MATHEMATICAL METHODS**

(COMMON TO EEE, ECE, CSE, EIE, BME, IT, E.CON.E CSS, ETM, ECC, ICE)

Time: 3hours

Max.Marks:80

**Answer any FIVE questions
All questions carry equal marks**

- 1.a) Find the positive root of $x^4 - x - 10 = 0$ by iteration.
 b) Find the value of Cos 1.747 using the values given in the table below: [8+8]

$x:$	1.70	1.74	1.78	1.82	1.86
$\sin x:$	0.9916	0.9857	0.9781	0.9691	0.9584

- 2.a) Fit a parabola of the form $y = a + bx + cx^2$ to the following data.

x	1	2	3	4	5	6	7
y	2.3	5.2	9.7	16.5	29.4	35.5	54.4

- b) A rocket is launched from the ground. Its acceleration is registered during the first 80 seconds and is given in the table below. Using Simpson's $\frac{1}{3}$ rd rule, find the velocity of the rocket at $t = 80$ seconds. [8+8]

t(sec)	0	10	20	30	40	50	60	70	80
f(cm/sec ²)	30	31.63	33.34	35.47	37.75	40.33	43.25	46.69	50.67

3. Given $y' = x^2(1+y)$ and $y(1) = 1$, $y(1.1) = 1.233$, $y(1.2) = 1.548$, $y(1.3) = 1.974$ estimate $y(1.4)$ using Milne's predictor-corrector method. [16]

- 4.a) Find the Rank of the matrix $A = \begin{bmatrix} 2 & 3 & -1 & -1 \\ 1 & -1 & -2 & -3 \\ 3 & 1 & 3 & -2 \\ 6 & 3 & 0 & -7 \end{bmatrix}$ by reducing it to the normal form.

- b) Solve the following system by the method of factorization $x + 3y + 8z = 4$; $x + 4y + 3z = -2$; $x + 3y + 4z = 1$. [8+8]

- 5.a) Find the eigen values and the corresponding eigen vectors of $\begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}$.

- b) Find the inverse of the matrix $\begin{bmatrix} 1 & -1 & 0 \\ 0 & 1 & 1 \\ 2 & 1 & 2 \end{bmatrix}$ using Cayley-Hamilton theorem. [8+8]

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6. Reduce the quadratic form $3x^2 + 5y^2 + 3z^2 - 2yz + 2zx - 2xy$ to the canonical form. [16]

7.a) Obtain Fourier series for the function $f(x)$ given by $f(x) = \begin{cases} -x, & \text{for } -\pi < x \leq 0 \\ x, & \text{for } 0 < x < \pi \end{cases}$

and deduce the value of $\frac{1}{1^2} + \frac{1}{2^2} + \frac{1}{3^2} + \dots$

b) Find the Fourier transform of the function [8+8]

$$f(x) = \begin{cases} 1 + \frac{x}{a} & \text{for } -a < x < 0 \\ 1 - \frac{x}{a} & \text{for } 0 < x < a \\ 0, & \text{otherwise} \end{cases}$$

8.a) Solve $q^2 y^2 = z(z - px)$.

b) Show that $z(\sinh n\theta) = \frac{z \sinh \theta}{z^2 - 2z \cosh \theta + 1}$. [8+8]

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SET-2

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- b) Solve the following system by the method of factorization $x + 3y + 8z = 4$; $x + 4y + 3z = -2$; $x + 3y + 4z = 1$. [8+8]

- 3.a) Find the eigen values and the corresponding eigen vectors of $\begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}$.

- b) Find the inverse of the matrix $\begin{bmatrix} 1 & -1 & 0 \\ 0 & 1 & 1 \\ 2 & 1 & 2 \end{bmatrix}$ using Cayley-Hamilton theorem. [8+8]

4. Reduce the quadratic form $3x^2 + 5y^2 + 3z^2 - 2yz + 2zx - 2xy$ to the canonical form. [16]

- 5.a) Obtain Fourier series for the function $f(x)$ given by $f(x) = \begin{cases} -x, & \text{for } -\pi < x \leq 0 \\ x, & \text{for } 0 < x < \pi \end{cases}$ and deduce the value of $\frac{1}{1^2} + \frac{1}{2^2} + \frac{1}{3^2} + \dots$

- b) Find the Fourier transform of the function [8+8]

$$f(x) = \begin{cases} 1 + \frac{x}{a} & \text{for } -a < x < 0 \\ 1 - \frac{x}{a} & \text{for } 0 < x < a \\ 0, & \text{otherwise} \end{cases}$$

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- 6.a) Solve $q^2 y^2 = z(z - px)$.
- b) Show that $z(\sinh n\theta) = \frac{z \sinh \theta}{z^2 - 2z \cosh \theta + 1}$. [8+8]
- 7.a) Find the positive root of $x^4 - x - 10 = 0$ by iteration.
 b) Find the value of Cos 1.747 using the values given in the table below: [8+8]

$x:$	1.70	1.74	1.78	1.82	1.86
$\sin x:$	0.9916	0.9857	0.9781	0.9691	0.9584

- 8.a) Fit a parabola of the form $y = a + bx + cx^2$ to the following data.

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- b) Find the inverse of the matrix $\begin{bmatrix} 1 & -1 & 0 \\ 0 & 1 & 1 \\ 2 & 1 & 2 \end{bmatrix}$ using Cayley-Hamilton theorem. [8+8]
2. Reduce the quadratic form $3x^2 + 5y^2 + 3z^2 - 2yz + 2zx - 2xy$ to the canonical form. [16]
- 3.a) Obtain Fourier series for the function $f(x)$ given by $f(x) = \begin{cases} -x, & \text{for } -\pi < x \leq 0 \\ x, & \text{for } 0 < x < \pi \end{cases}$
and deduce the value of $\frac{1}{1^2} + \frac{1}{2^2} + \frac{1}{3^2} + \dots$
- b) Find the Fourier transform of the function [8+8]

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- 4.a) Solve $q^2 y^2 = z(z - px)$.
- b) Show that $z(\sinh n\theta) = \frac{z \sinh \theta}{z^2 - 2z \cosh \theta + 1}$. [8+8]
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- b) Solve the following system by the method of factorization $x + 3y + 8z = 4$; $x + 4y + 3z = -2$; $x + 3y + 4z = 1$.

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- b) Find the Fourier transform of the function

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